

# DAMAGE DETECTION USING THE HOLDER EXPONENT



Mackinac Bridge, MI, USA

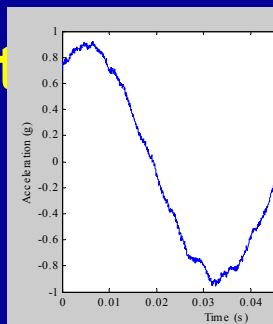
([www.worldstart.com](http://www.worldstart.com))

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Scott R. Green  
Timothy A. Schwartz  
Mentor – Charles R. Farrar

Dynamics Summer School  
August 1, 2002

# Overview

- ◆ Motivation
- ◆ Background and previous
- ◆ Our endeavor
- ◆ Results and next



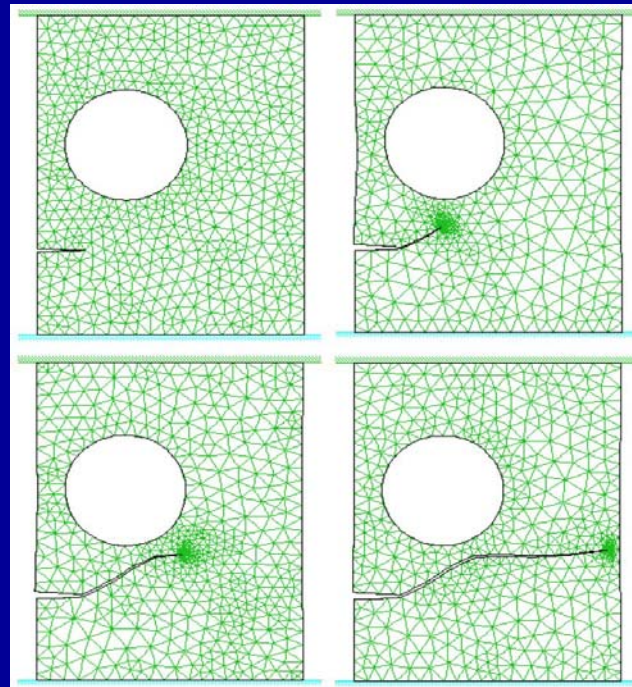
Courtesy of the Navy Research Lab

# Damage introduces non-linearities in a structural system

Crack initiation and propagation

Bolt pretension loss

Loose part “rattle”



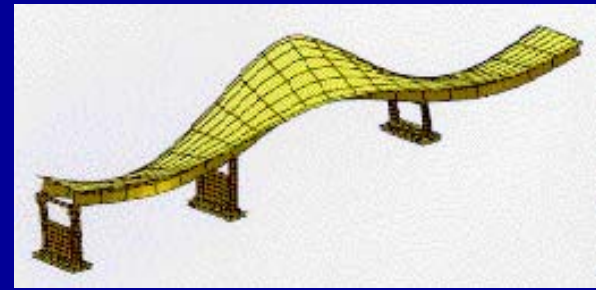
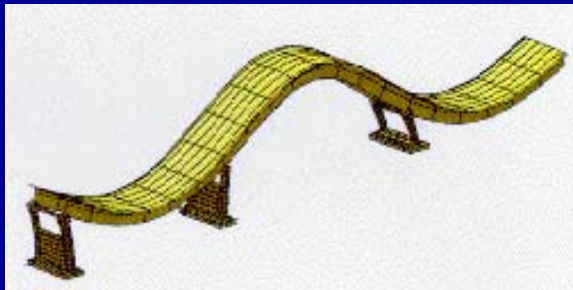
[www-cemef.cma.fr](http://www-cemef.cma.fr)





# Current detection methods characterize changes in linear models of the structure

## ◆ Modal shapes and parameters



[www.lanl.gov](http://www.lanl.gov)

## ◆ Autoregressive correlation coefficients



# However, these methods are not foolproof

- ◆ Modal analysis methods only detect global changes
- ◆ Autoregressive models do not take advantage of non-linearities

Monitoring of structural health should involve pinpointing damage:

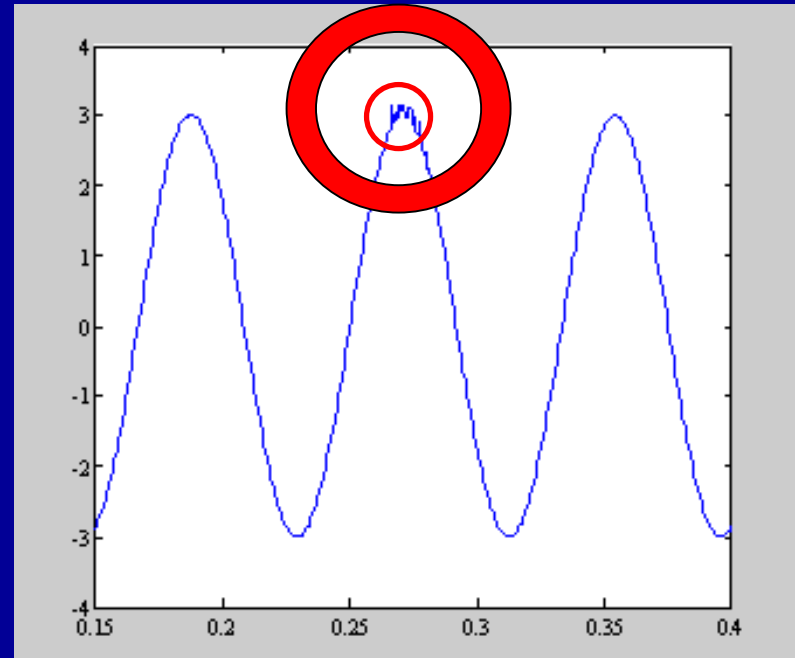
- ◆ In time
- ◆ In space



# A damage detection method using a feature known as the Holder Exponent is explored

## How?

- ◆ Measures time signal regularity
- ◆ Extracts instantaneous high frequency content

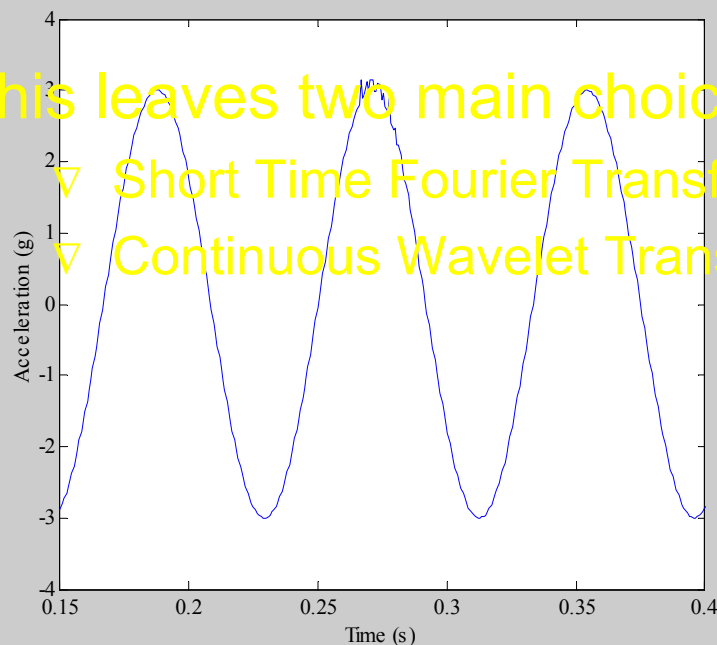


# Calculation of the Holder Exponent relies on time-frequency analysis methods

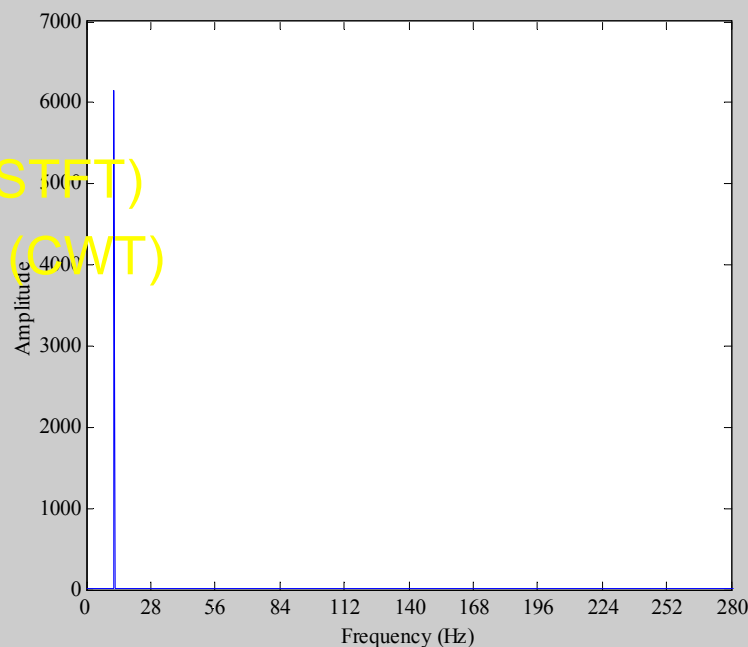
## Fast Fourier Transform (FFT) shortcomings

This leaves two main choices:

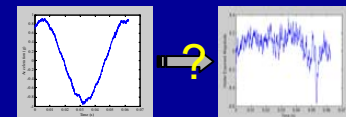
- ▽ Short Time Fourier Transform (STFT)
- ▽ Continuous Wavelet Transform (CWT)



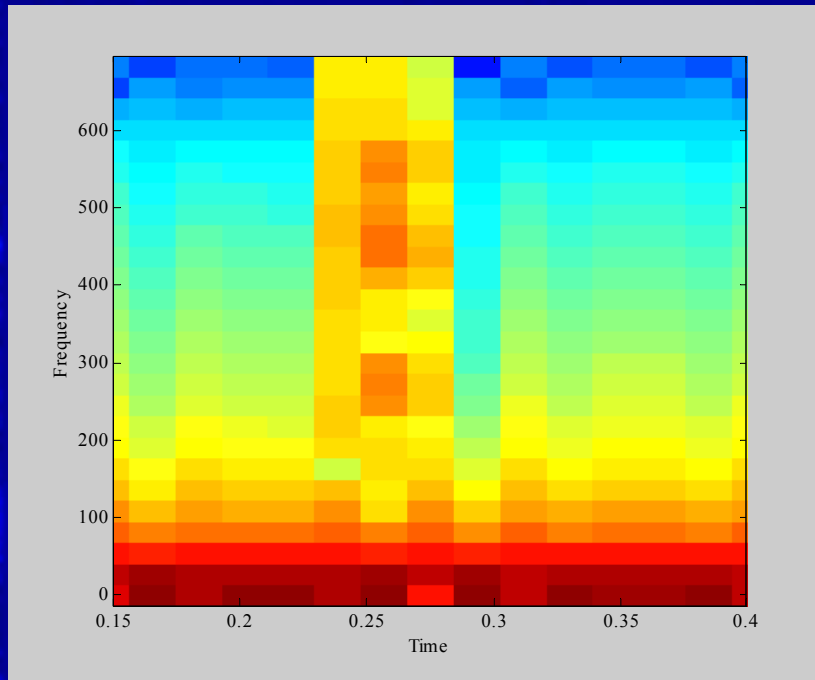
Time signal



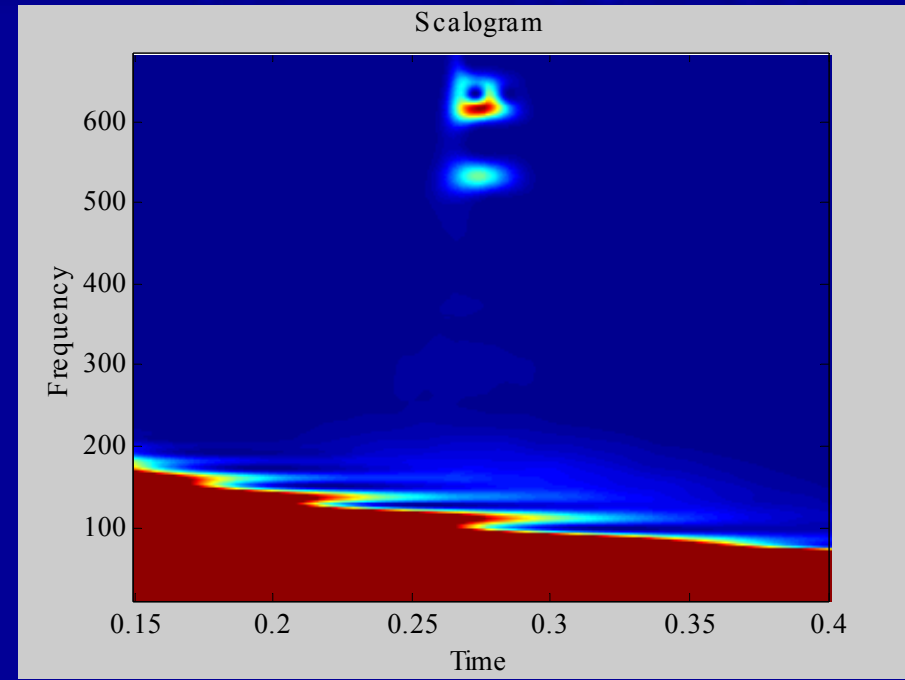
FFT



# The important difference between the STFT and the CWT lies in resolution

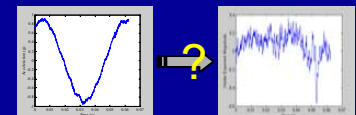


STFT



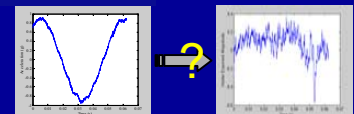
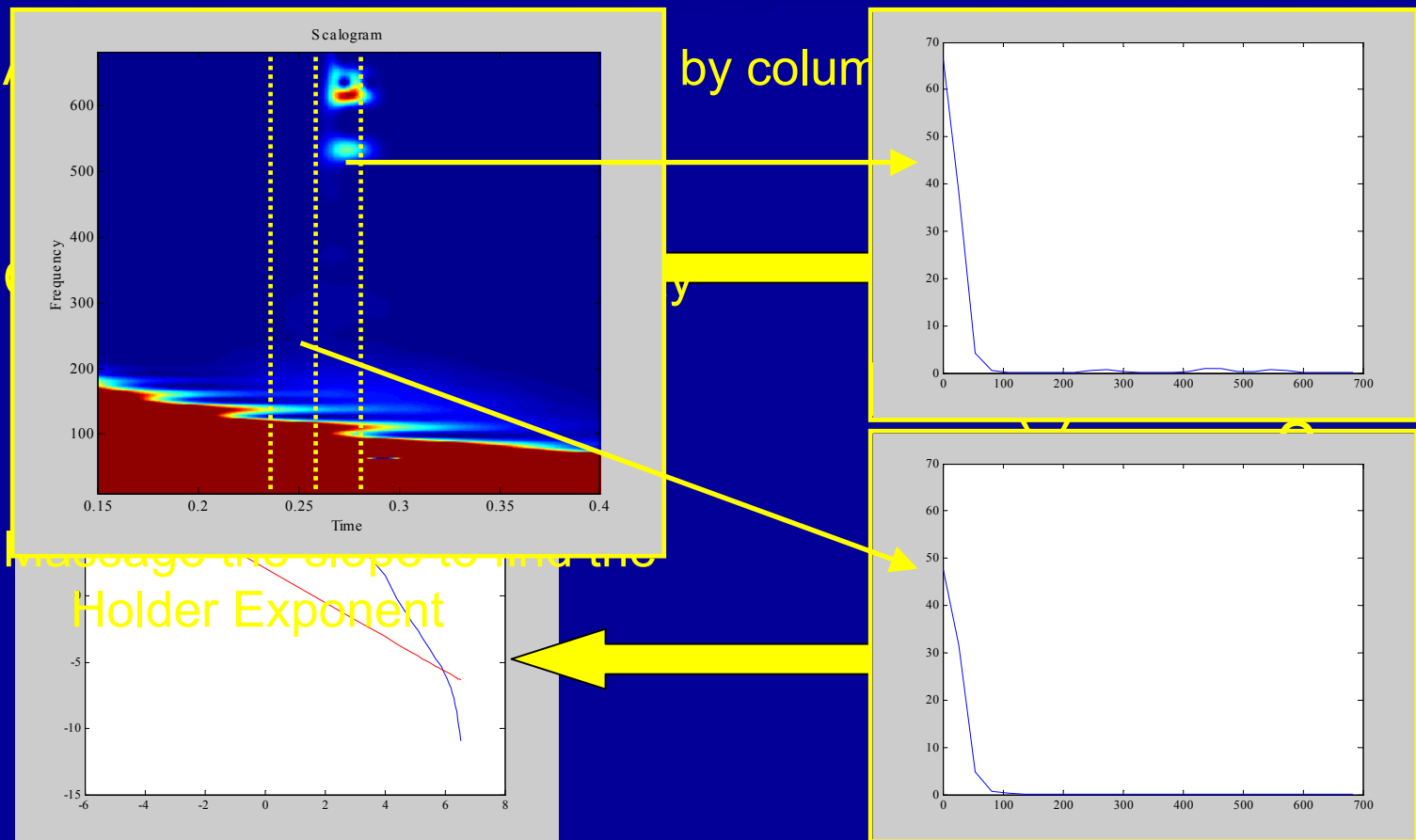
CWT

The excellent time resolution at high frequencies is key



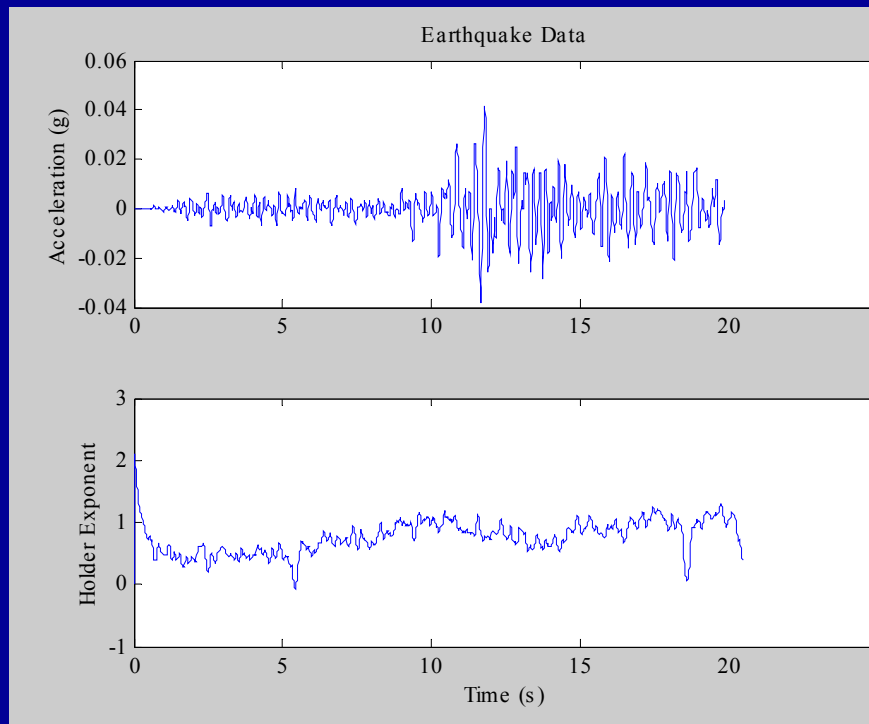


# The Holder Exponent can be computed directly from the CWT

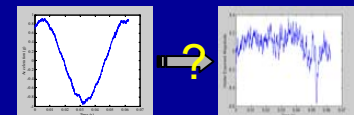
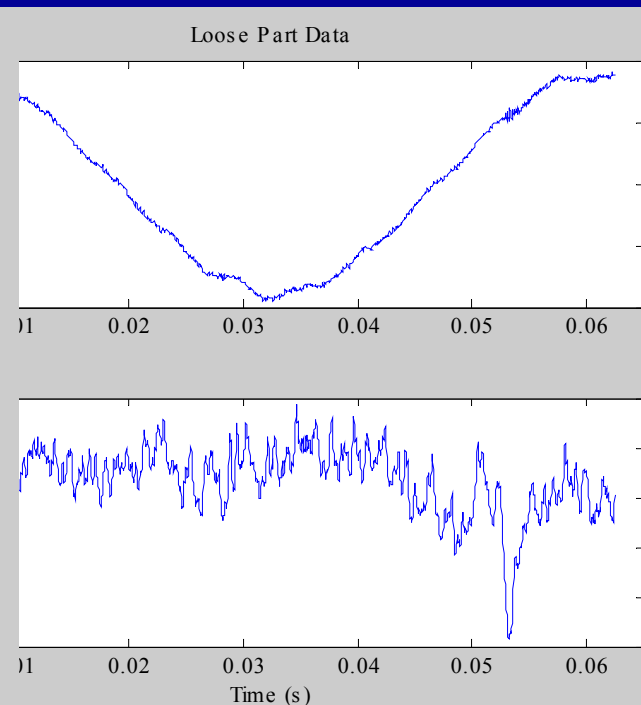


# Robertson and Farrar first explored the capability of the Holder Exponent

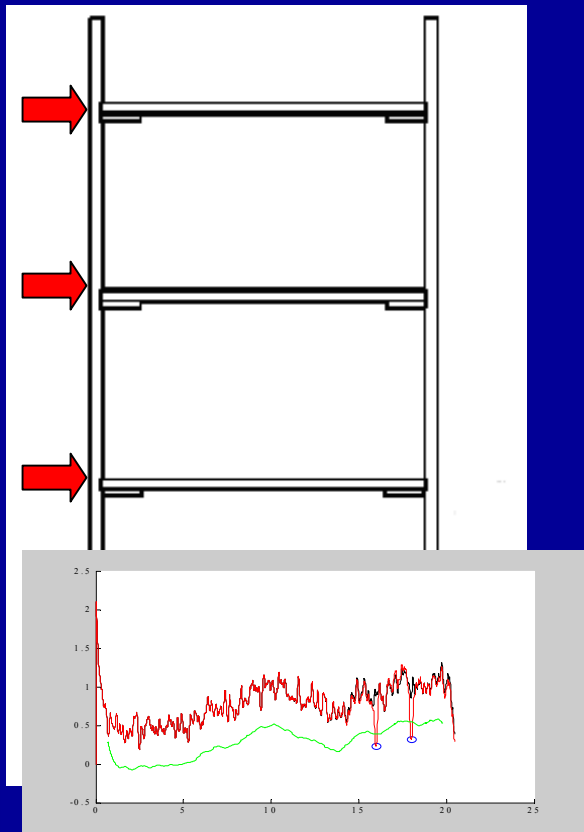
## Doctored earthquake data



## Loose part rattle



# The effectiveness of the Holder Exponent is explored by testing physical models



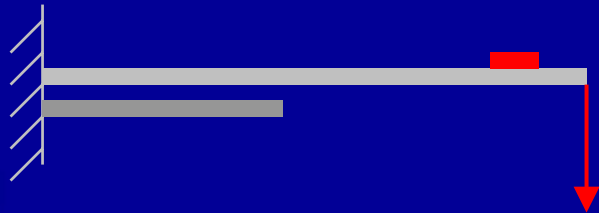
Applicability to “real world” structures

Sensitivity to instrument locations

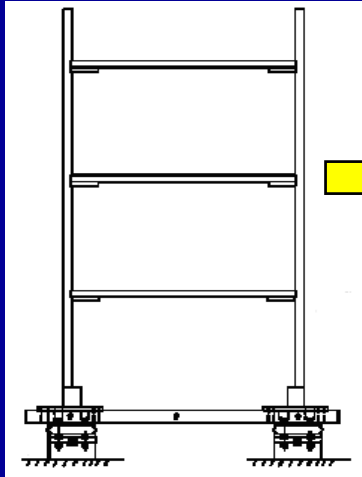
Automating the detection process with a Statistical Process Control (SPC)



# The tested structures modeled different forms of damage



Cantilever beam



Three-story structure

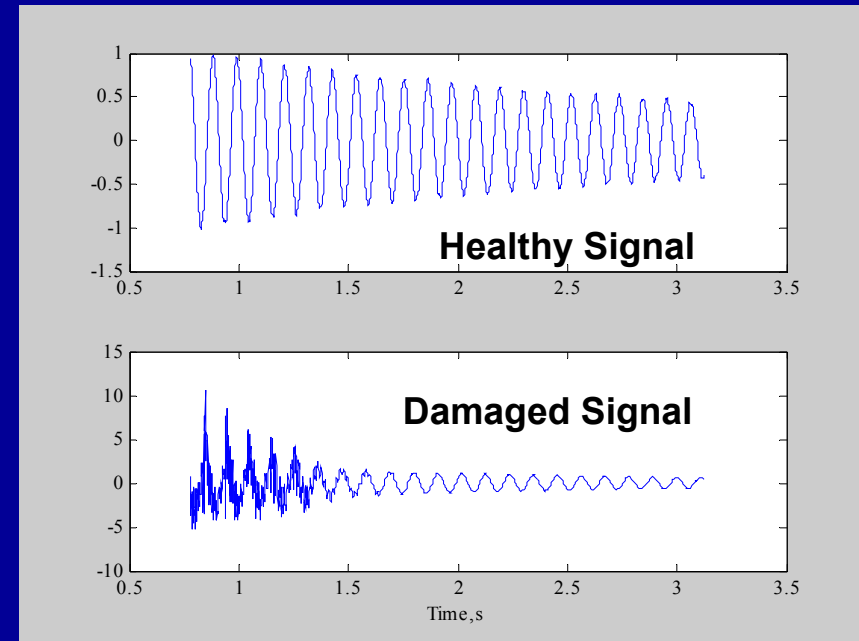
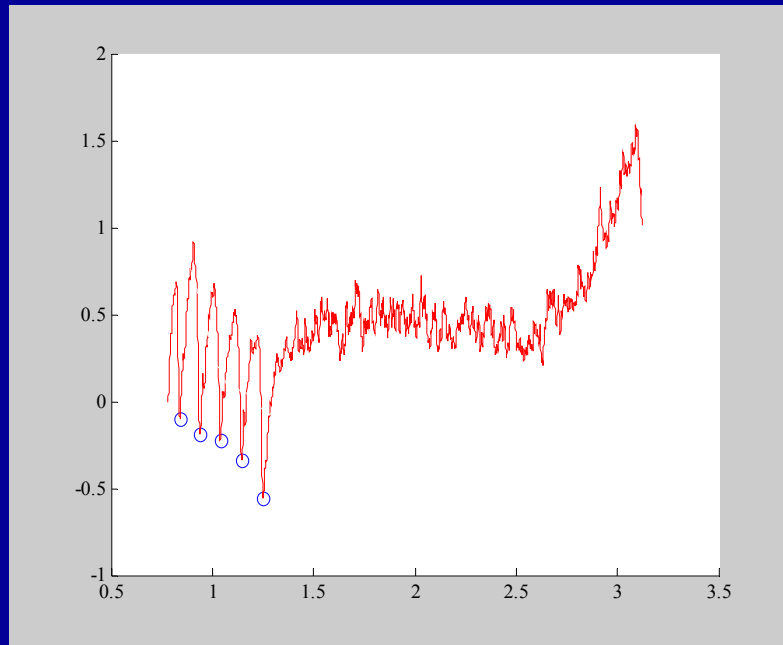


5 DOF system





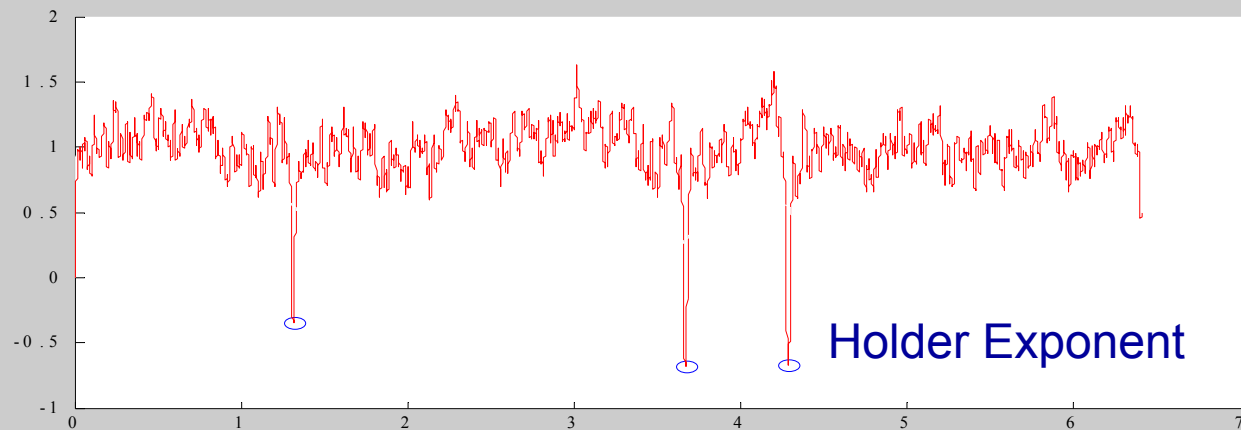
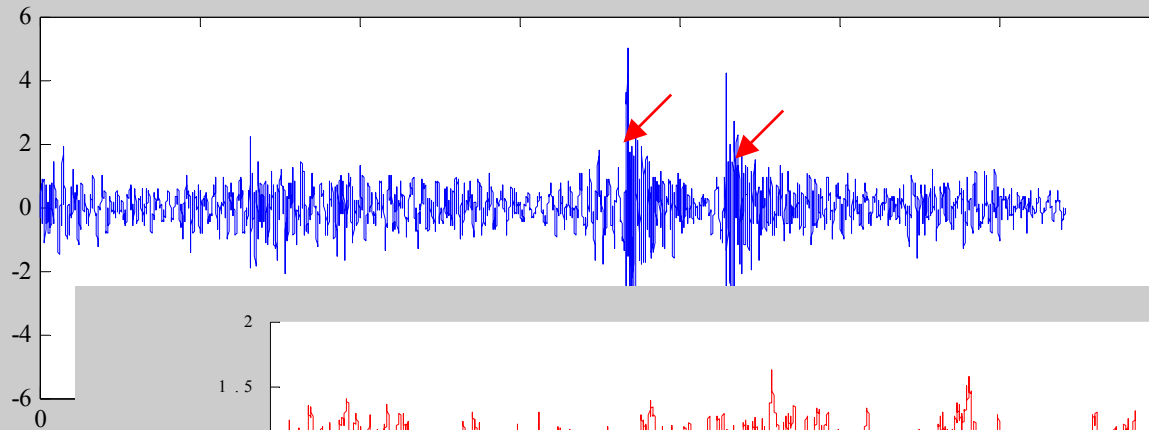
# Results from the cantilever beam showed the Holder Exponent was sensitive to damage



However, obvious events do not really need detection methods



The Holder Exponent detected damage in the 5 DOF,  
but some features were obvious in the time signal



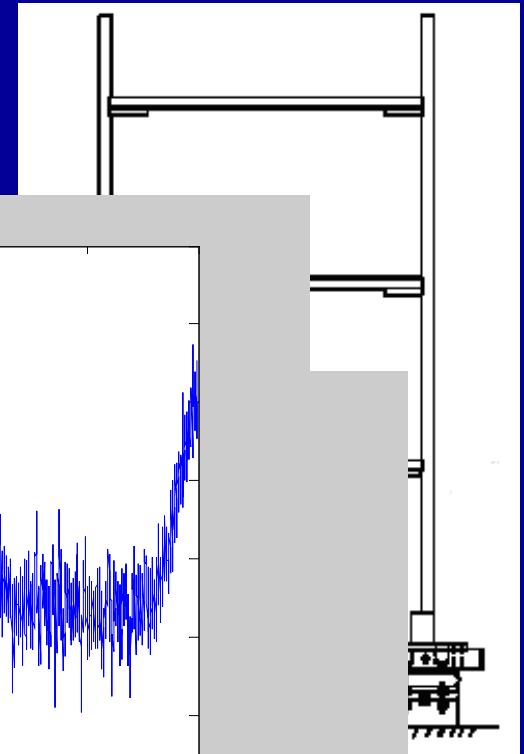
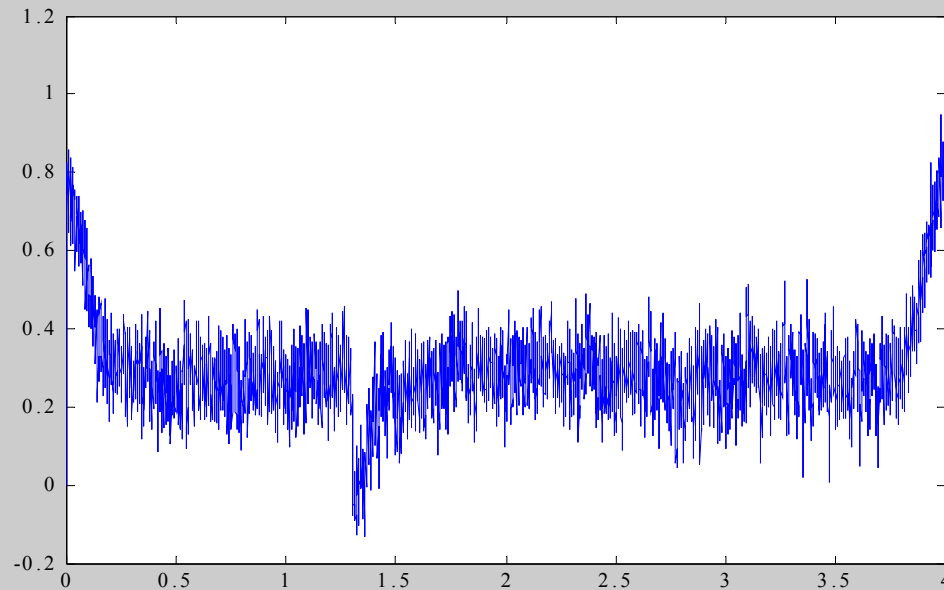
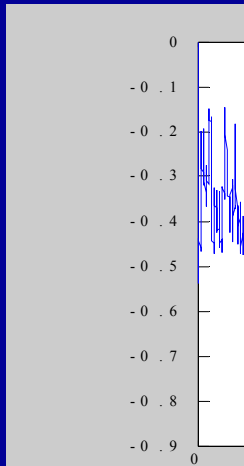
Magnitudes and occurrences of the impacts were  
difficult to control



The three-story structure produced varying results based on the input

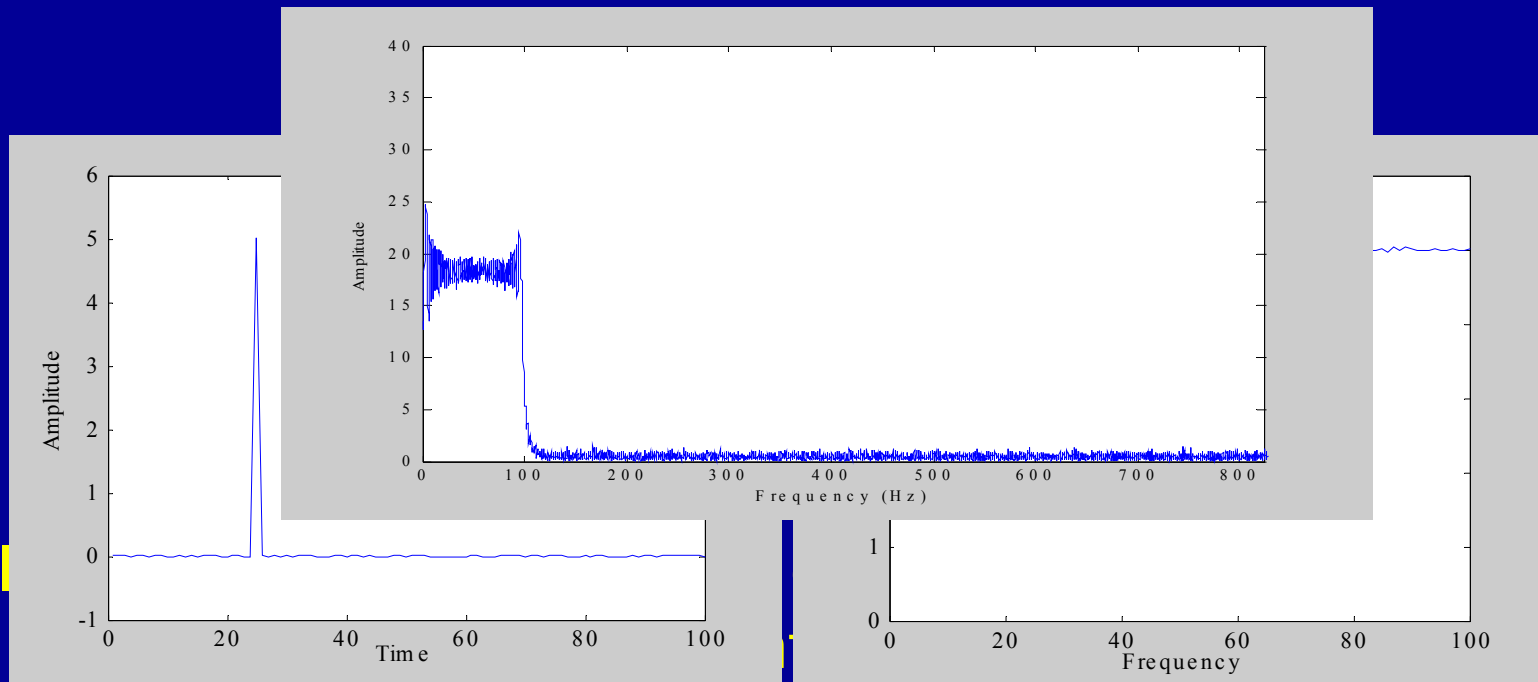
The Holder Exponent is effective for periodic inputs

The Holder Exponent is effective for broadband inputs



# A return to the fundamentals illuminated why random inputs were not giving favorable results

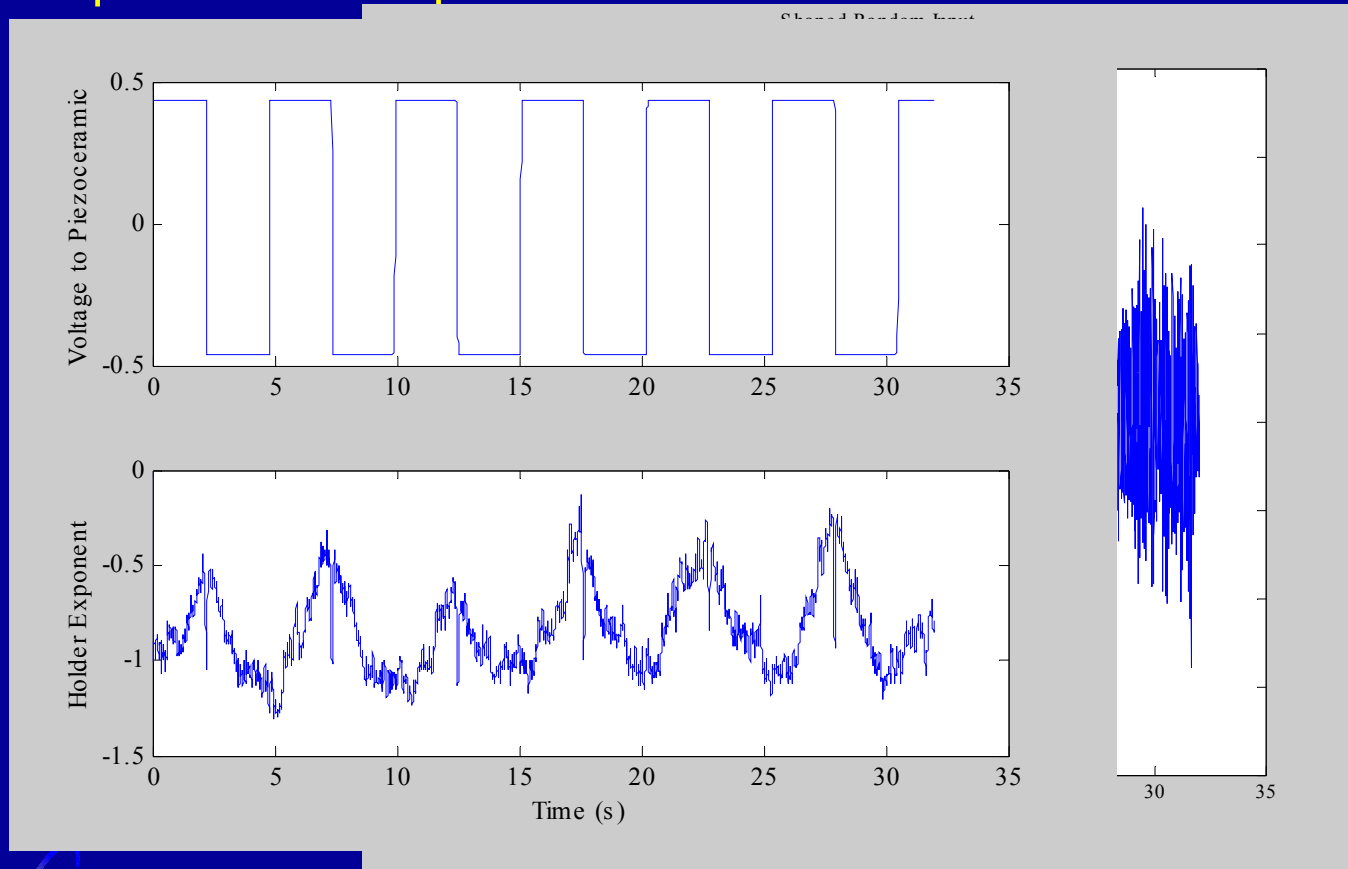
## Frequency content of impulse is broadband





# Armed with this insight, the three-story structure was revisited

## Shaped random input



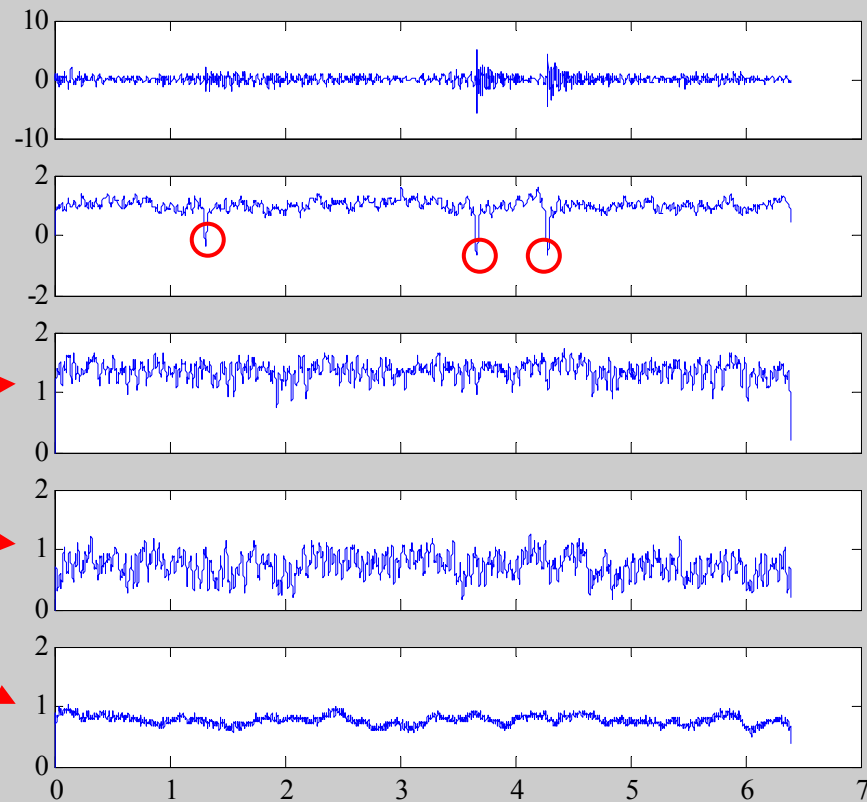
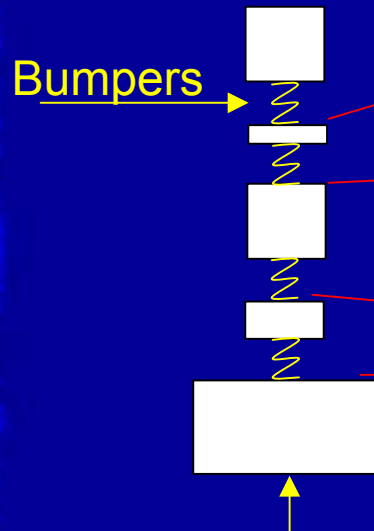
ing results for  
world  
lications



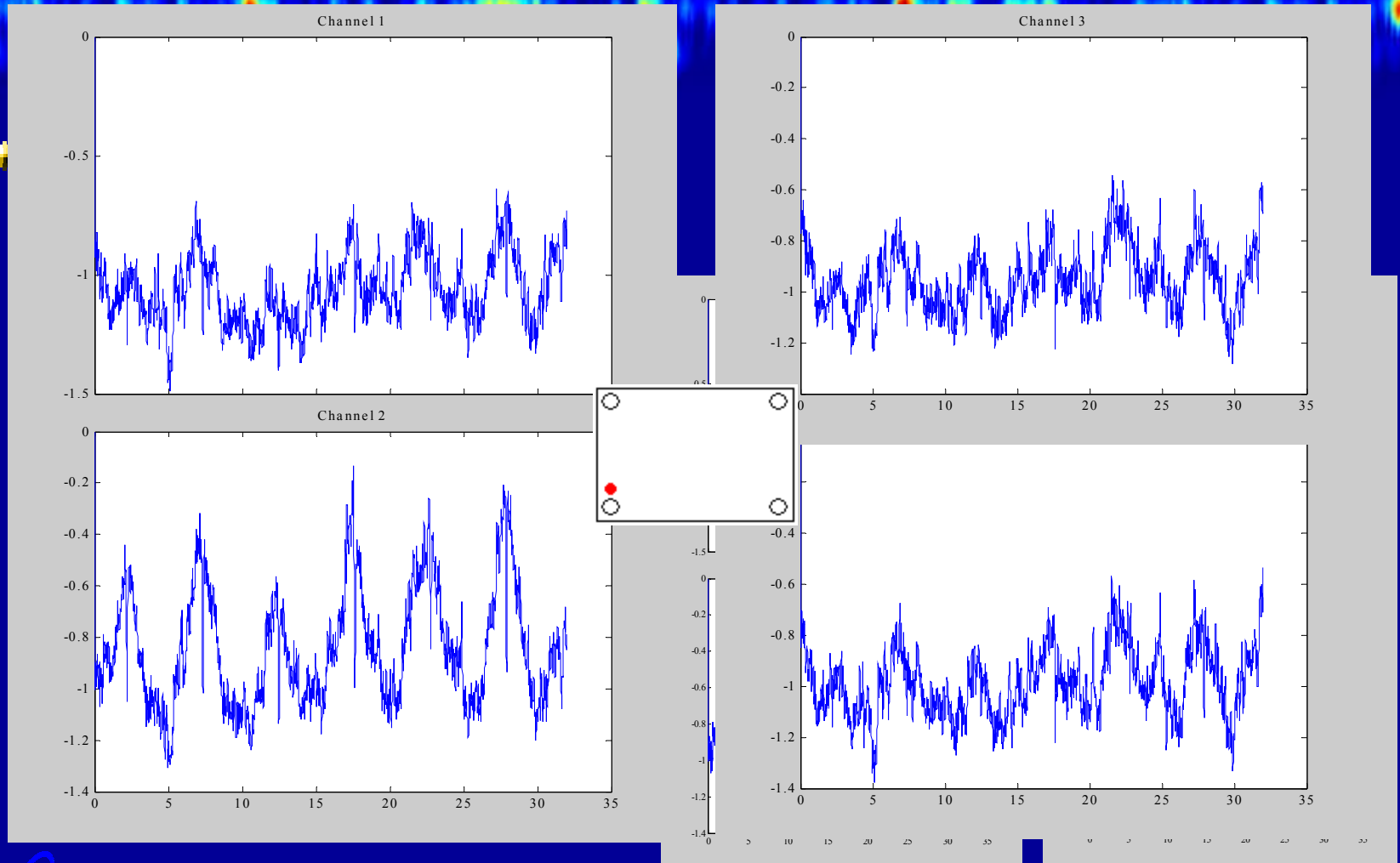
# Subsequently, the sensitivity to proximity was explored

## 5-DOF system:

✦ Limited sensitivity

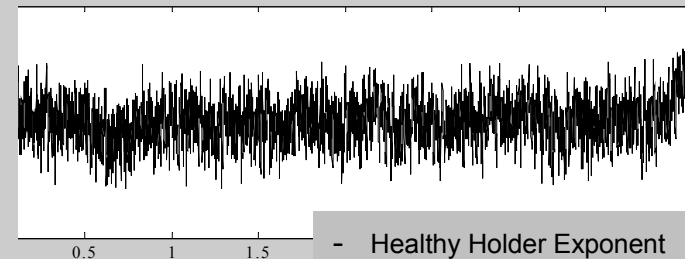
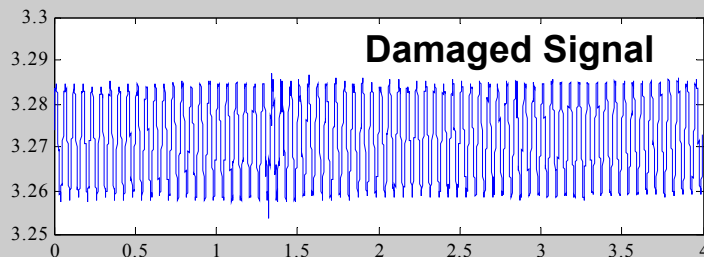
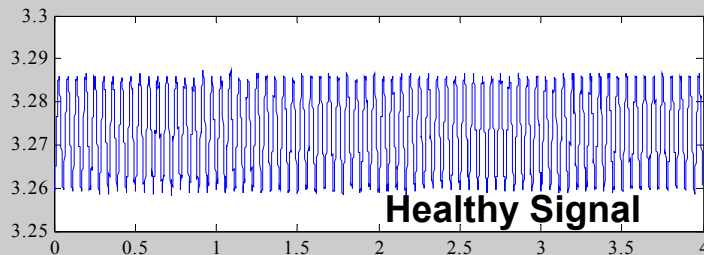


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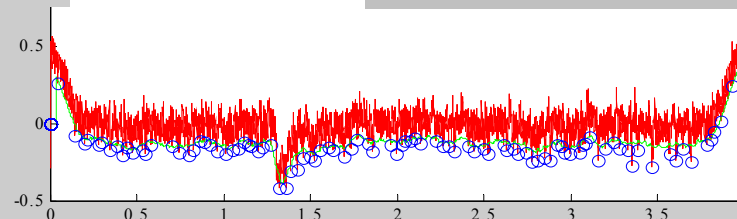


# A SPC was developed to assess the feasibility of automating the detection scheme

## Establishment of control limits



- Healthy Holder Exponent
- Damaged Holder Exponent
- o Discontinuity
- Control Limit



Best results when healthy data is used





# Significant discoveries were made with regards to the usefulness of the Holder Exponent

- ◆ Frequency content of the input is important
- ◆ Information from damage events is attenuated
- ◆ Automating the detection process seems to hold promise

## The applicability of the Holder Exponent could be further characterized

- ◆ Sensitivity to damage level
- ◆ Quantify proximity sensitivity for more systems



# Acknowledgments

- ◆ Special thanks to Jeanette Wait for procedural and data extraction help
- ◆ Thanks to Amy Robertson and Hoon Sohn for aiding in our understanding of the fundamentals
- ◆ Thanks to the Engineering Science and Applications Division at the Los Alamos National Laboratory and the Dept. of Energy's Education Programs Office for funding
- ◆ Thanks to The Mathworks, Inc. for generously donating numerical analysis software

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## QUESTIONS?

